# Theoretical Study of Ruthenium-Catalyzed Hydrogenation of Carbon Dioxide into Formic Acid. Reaction Mechanism Involving a New Type of $\sigma$-Bond Metathesis 

Yasuo Musashi*, ${ }^{*}$ and Shigeyoshi Sakaki*,*<br>Contribution from the Information Processing Center, Kumamoto University, Kumamoto 860-8555, Japan, and Department of Applied Chemistry and Biochemistry, Faculty of Engineering, Kumamoto University, Kumamoto 860-8555, Japan

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#### Abstract

Ruthenium-catalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid was theoretically investigated with the $\mathrm{DFT}(\mathrm{B} 3 \mathrm{LYP})$ method, where cis $-\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ was adopted as a catalyst model. Theoretical calculations show that (1) $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond occurs with an activation energy ( $E_{\mathrm{a}}$ ) of $29.3 \mathrm{kcal} / \mathrm{mol}$ in cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ and with an $E_{\mathrm{a}}$ value of $10.3 \mathrm{kcal} / \mathrm{mol}$ in cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}$; $(2)$ six-membered $\sigma$-bond metathesis of $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right)$ occurs with a much smaller $E_{\mathrm{a}}$ value $(8.2 \mathrm{kcal} / \mathrm{mol})$ than four-membered $\sigma$-bond metathesis ( $E_{\mathrm{a}}=24.8 \mathrm{kcal} / \mathrm{mol}$ ) and five-membered $\mathrm{H}-\mathrm{OCOH}$ reductive elimination ( $E_{\mathrm{a}}=25.5 \mathrm{kcal} / \mathrm{mol}$ ); (3) three-membered $\mathrm{H}-\mathrm{OCOH}$ reductive elimination requires a very much larger $E_{\mathrm{a}}$ value of $43.2 \mathrm{kcal} / \mathrm{mol}$; (4) if $\mathrm{PH}_{3}$ dissociates from cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$, the $\mathrm{CO}_{2}$ hydrogenation takes place through the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}$ followed by the six-membered $\sigma$-bond metathesis, where the rate-determining step is the $\mathrm{CO}_{2}$ insertion; and (5) if $\mathrm{PH}_{3}$ does not dissociate from cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ and cis- $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)-$ $\left(\mathrm{PH}_{3}\right)_{4}$, the $\mathrm{CO}_{2}$ hydrogenation proceeds through the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of $c i s-\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ followed by the $\mathrm{H}-\mathrm{OCOH}$ reductive elimination, where the rate-determining step is the $\mathrm{CO}_{2}$ insertion. From the above conclusions, one might predict that (1) excess phosphine suppresses the reaction, (2) the use of solvent that facilitates phosphine dissociation is recommended, and (3) the ruthenium(II) complex with three phosphine ligands is expected to be a good catalyst. The electronic processes and characteristic features of the $\mathrm{CO}_{2}$ insertion reaction and the $\sigma$-bond metathesis are discussed in detail.


## 1. Introduction

$\mathrm{CO}_{2}$ fixation is an important subject of research in organometallic and catalytic chemistries. ${ }^{1}$ One of the most attractive and interesting reactions of $\mathrm{CO}_{2}$ fixation is transition metal catalyzed $\mathrm{CO}_{2}$ hydrogenation into formic acid, ${ }^{2-6}$ because formic acid is often used as a raw material in organic syntheses. Such transition metal complexes as $\left[\mathrm{WH}(\mathrm{CO})_{5}\right]^{-},{ }^{7} \mathrm{RhH}(\mathrm{P}-\mathrm{P})_{2}$ ( $\mathrm{P}-\mathrm{P}=1,2$-bis(diphenylphosphino)ethane or 1,3-bis(diphenylphosphino)propane $),{ }^{8}\left[\mathrm{RhH}_{2}\left(\mathrm{PMe}_{2} \mathrm{Ph}\right)_{3}(\mathrm{~L})\right]^{+}\left(\mathrm{L}=\mathrm{H}_{2} \mathrm{O}\right.$ or THF), ${ }^{9}$ and cis- $\mathrm{RuH}_{2}\left(\mathrm{PR}_{3}\right)_{4}\left(\mathrm{R}=\mathrm{Me}^{10}\right.$ or $\left.\mathrm{Ph}^{11}\right)$ were used as catalysts of this reaction. Tsai and Nicholas experimentally investigated a hydrogenation reaction of $\mathrm{CO}_{2}$ catalyzed by

[^0]$\left[\mathrm{RhH}_{2}\left(\mathrm{PMe}_{2} \mathrm{Ph}\right)_{3}(\mathrm{~L})\right]^{+}$and spectroscopically detected $\mathrm{Rh}(\mathrm{III}) \eta^{1}-$ formate and Rh (III) $\eta^{2}$-formate complexes. ${ }^{9}$ From these results, they proposed that the reaction proceeded through $\mathrm{CO}_{2}$ insertion into the $\mathrm{Rh}(\mathrm{III})-\mathrm{H}$ bond of $\left[\mathrm{RhH}_{2}\left(\mathrm{PMe}_{2} \mathrm{Ph}\right)_{3}(\mathrm{~L})\right]^{+}$followed by reductive elimination of formic acid from $\left[\mathrm{RhH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PMe}_{2}-\right.\right.$ $\left.\mathrm{Ph})_{3}(\mathrm{~L})\right]^{+}(\mathrm{L}=$ solvent $)$. Also, Leitner found that the $\mathrm{Rh}(\mathrm{I})$ hydride complex, $\mathrm{RhH}(\mathrm{P}-\mathrm{P})$, catalyzed the hydrogenation of $\mathrm{CO}_{2}$ into formic acid. ${ }^{8}$ Later, Hutschka et al. experimentally and theoretically investigated this catalytic reaction in detail and proposed that this reaction took place through the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Rh}(\mathrm{I})-\mathrm{H}$ bond of $\mathrm{RhH}\left(\mathrm{PH}_{3}\right)_{2}$ followed by the $\sigma$-bond metathesis of $\mathrm{Rh}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{2}$ with molecular hydrogen. ${ }^{12}$ Recently, Jessop, Ikariya, and Noyori succeeded in significantly efficient hydrogenation of $\mathrm{CO}_{2}$ into formic acid with $\mathrm{Ru}(\mathrm{II})$ complexes in supercritical $\mathrm{CO}_{2}$ (eq 1). ${ }^{10}$ The extremely high
\[

$$
\begin{equation*}
\left.\mathrm{CO}_{2}+\mathrm{H}_{2} \xrightarrow[\text { in scCO}]{2}, \mathrm{~N}\left(\mathrm{C}_{2} \mathrm{H}_{5}\right)_{3}\right) ~ \mathrm{cis}_{2}-\mathrm{RuH}_{2}\left(\mathrm{PMe}_{2}\right)_{4} \mathrm{HCO}_{2} \tag{1}
\end{equation*}
$$

\]

catalytic activity of the $\mathrm{Ru}(\mathrm{II})$ complex motivates us to investigate theoretically the Ru-catalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid, since it is considerably interesting and important to clarify the reaction mechanism and the ratedetermining step of $\mathrm{Ru}(\mathrm{II})$-catalyzed hydrogenation of $\mathrm{CO}_{2}$.

In the present work, all the elementary steps involved in the catalytic cycle of $\mathrm{Ru}(\mathrm{II})$-catalyzed hydrogenation of $\mathrm{CO}_{2}$ into

[^1]formic acid are theoretically investigated with the density functional theory (DFT) method. Our purposes here are (1) to elucidate the reaction mechanism, (2) to show what is the ratedetermining step, and (3) to provide detailed knowledge of characteristic features of this reaction. Our intention here is to present a clear conclusion of the reaction mechanism and to indicate the importance of six-membered $\sigma$-bond metathesis of $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{n}(n=3$ or 4$)$ with $\mathrm{H}_{2}$. This six-membered $\sigma$-bond metathesis is significantly different from the fourmembered $\sigma$-bond metathesis proposed recently, ${ }^{12}$ but similar to formate-assisted six-membered $\mathrm{H}_{2}$ splitting which was previously proposed by Darensbourg et al. ${ }^{7}$ in the hydrogenation of $\mathrm{CO}_{2}$ into formic acid catalyzed by $\left[\mathrm{WH}(\mathrm{CO})_{5}\right]^{-}$but has received little attention so far. Similar $\mathrm{H}_{2}$ splitting assisted by a ligand has also been reported by Morris et al., ${ }^{13}$ Crabtree et al. ${ }^{14}$ and Milet et al. ${ }^{15}$

## 2. Catalyst Model and Examined Reactions

Since a ruthenium(II) complex, $\mathrm{RuH}_{2}\left(\mathrm{PMe}_{3}\right)_{4}$, was used as a catalyst in $\mathrm{Ru}(\mathrm{II})$-catalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid, ${ }^{10}$ we adopted here cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ as a catalyst model. Komiya et al. ${ }^{16}$ and Kolomnikov et al. ${ }^{17}$ experimentally reported that the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of cis $-\mathrm{RuH}_{2}\left(\mathrm{PR}_{3}\right)_{4}$ (1) occurred with phosphine dissociation when $\mathrm{PPh}_{3}$ was used as a ligand. On the other hand, Jessop et al. reported that addition of $\mathrm{PMe}_{3}$ did not suppress the stoichiometric $\mathrm{CO}_{2}$ insertion in cis- $\mathrm{RuH}_{2}\left(\mathrm{PMe}_{3}\right)_{4} .{ }^{10 \mathrm{c}}$ This result suggests that $\mathrm{CO}_{2}$ is inserted into the $\mathrm{Ru}-\mathrm{H}$ bond without $\mathrm{PMe}_{3}$ dissociation. Several reports suggested that a bulky phosphine tends to dissociate from the central metal. ${ }^{18}$ Thus, we investigated two types of $\mathrm{CO}_{2}$ insertion; one is the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of a six-coordinate $\mathrm{Ru}(\mathrm{II})$ complex, cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ (1a) (eq 2a), without $\mathrm{PH}_{3}$ dissociation, and the other is the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of a five-coordinate $\mathrm{Ru}(\mathrm{II})$ complex, cis$\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}(\mathbf{1 b})$ (eq 2b), with $\mathrm{PH}_{3}$ dissociation.

$$
\begin{align*}
& \text { cis- } \mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}+\mathrm{CO}_{2} \rightarrow \mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{4}  \tag{2a}\\
& \text { cis- } \mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}+\mathrm{CO}_{2} \rightarrow \operatorname{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}  \tag{2b}\\
& \mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{n} \rightarrow \mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{n}(\mathrm{HCOOH}) \text { or } \\
& \quad(n=3 \text { or } 4)
\end{align*}
$$

$$
\begin{equation*}
\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{4}+\mathrm{HCOOH} \tag{3}
\end{equation*}
$$

$\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{4}(\mathrm{HCOOH})+\mathrm{H}_{2} \rightarrow$

$$
\begin{equation*}
\text { cis }-\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}+\mathrm{HCOOH} \tag{4}
\end{equation*}
$$

$\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{4}+\mathrm{H}_{2} \rightarrow$ cis $-\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$
$\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{4}+\mathrm{H}_{2} \rightarrow$

$$
c i s-\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right)+\mathrm{PH}_{3}
$$

$$
\rightarrow \mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}(\mathrm{HCOOH})+\mathrm{PH}_{3}(6 \mathrm{a})^{19}
$$

$$
\begin{aligned}
& \operatorname{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}+\mathrm{H}_{2} \rightarrow \\
& \text { cis-RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right)
\end{aligned}
$$

$$
\rightarrow \mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}(\mathrm{HCOOH}) \quad(6 \mathrm{~b})^{19}
$$

Two reaction courses are considered possible in the formation of formic acid from a formate complex, $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{n}$ ( $n=3$ or 4 ); one is the reductive elimination of formic acid from $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{n}$, to yield $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{n}(\mathrm{HCOOH})$ (eq 3 ). In this case, the ruthenium dihydride complex of an active
species must be reproduced through the oxidative addition of $\mathrm{H}_{2}$ to a $\mathrm{Ru}(0)$ complex, $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{n}(\mathrm{HCOOH})$ or $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{n}$ (eqs 4 and 5). The other is the $\sigma$-bond metathesis of $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)$ $\left(\mathrm{PH}_{3}\right)_{n}$ with a hydrogen molecule (eqs 6a and 6b). To perform the $\sigma$-bond metathesis, $\mathrm{H}_{2}$ must coordinate with Ru . When $n=$ 4, $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{4}$ possesses no room for $\mathrm{H}_{2}$ coordination, and therefore, substitution of $\mathrm{H}_{2}$ for $\mathrm{PH}_{3}$ must occur to yield $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right)$, as shown in eq 6 a . When $n$ $=3, \mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}$ has an unoccupied coordination site, and therefore, $\mathrm{H}_{2}$ easily coordinates with Ru to afford RuH -$\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right)$, as shown in eq 6 b . We investigated here six-membered $\sigma$-bond metathesis and four-membered $\sigma$-bond metathesis in $\operatorname{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right)$. When the $\sigma$-bond metathesis takes place, the active species of cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}$ is produced concomitantly with the formation of HCOOH , and therefore, the oxidative addition of $\mathrm{H}_{2}$ to a $\mathrm{Ru}(0)$ complex does not need to occur.

## 3. Computations

The density functional theory (DFT) method ${ }^{20}$ was employed here with the B3LYP functional for the exchange correlation term. ${ }^{21,22}$ Geometries were optimized with the following basis set system (BSI): core electrons of P (up to 2 p ) and Ru (up to 3d) were replaced with effective core potentials (ECPs), and their valence electrons were represented with $(21 / 21 / 1)$ and ( $311 / 311 / 211$ ) sets, respectively. ${ }^{23,24}$ MIDI-4 sets ${ }^{25}$ were employed for C and O , and a (4s)/[2s] set ${ }^{26}$ was used for H . A d-polarization function ${ }^{25}$ was added on C and O , and a p-polarization function ${ }^{26}$ was added on the active hydrogen atom that was hydride and the H atom of formate. Energy changes ${ }^{27}$ were calculated with a better basis set system (BS-II), using DFT(B3LYP)/ BS-I optimized geometries. In BS-II, a $(541 / 541 / 211)^{28}$ set was employed for Ru with the same ECPs as those in BS-I. ${ }^{24}$ A MIDI-4 set ${ }^{25}$ was used for P , where a d-polarization function was added. ${ }^{25}$ For C and $\mathrm{O},(9 \mathrm{~s} 5 \mathrm{p} 1 \mathrm{~d}) /[3 \mathrm{~s} 2 \mathrm{p} 1 \mathrm{~d}] \mathrm{sets}^{26}$ were used with a p-diffuse function. ${ }^{26}$ For the active H atom, a ( 5 s 1 p )/[ 3 s 1 p$] \mathrm{set}^{29}$ was employed.
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Figure 1. Geometry changes in the insertion of $\mathrm{CO}_{2}$ into the $\mathrm{Ru}-\mathrm{H}$ bond of cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{n}(n=3$ and 4$)$. Bond distances are in angstroms and bond angles in degrees. In parentheses are the energy differences from $\mathbf{1 a}$ ( $\mathrm{kcal} / \mathrm{mol}$; DFT (B3LYP)/BS-II//DFT(B3LYP)/BS-I calculation). The $\mathrm{P}^{1} \mathrm{H}_{3}$ and $\mathrm{P}^{2} \mathrm{H}_{3}$ ligands, which are perpendicular to the $\mathrm{P}^{3}-\mathrm{Rh}-\mathrm{H}^{1}$ plane, are omitted for brevity because the $\mathrm{Ru}-\mathrm{P}^{1}$ and $\mathrm{Ru}-\mathrm{P}^{2}$ distances hardly change through the hydrogenation of $\mathrm{CO}_{2}$.

All the transition states were ascertained by vibrational frequency calculation with the DFT(B3LYP)/BS-I method. Gaussian 94 and 98 programs were used in these calculations. ${ }^{30,31}$

[^2]
## 4. Results and Discussion

4.1. The $\mathrm{CO}_{2}$ Insertion into the $\mathbf{R u}-\mathbf{H}$ Bond of $\mathbf{R u H}_{\mathbf{2}^{-}}$ $\left(\mathbf{P H}_{3}\right)_{n}$ ( $n=3$ or 4). Geometry changes in the $\mathrm{CO}_{2}$ insertion reaction are shown in Figure 1. cis $-\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ 1a takes a sixcoordinate pseudo-octahedral structure. The optimized $\mathrm{Ru}-\mathrm{H}$ bond distance $(1.615 \AA$ ) is within a range of experimental values: $1.630 \AA$ in $\mathrm{RuH}\left(\eta^{5}-\mathrm{C}_{5} \mathrm{H}_{5}\right)\left(\mathrm{PMe}_{3}\right)_{2}$ and $1.602 \AA$ (average) in $\left[\mathrm{RuH}_{2}\left(\eta^{5}-\mathrm{C}_{5} \mathrm{H}_{5}\right)\left(\mathrm{PMe}_{3}\right)_{2}\right]^{+} .{ }^{32}$ The similar $\mathrm{Ru}-\mathrm{H}$ distance was previously reported in a theoretical investigation of $\mathrm{RuH}_{2}-$ $\left(\mathrm{PH}_{3}\right)_{4} \cdot{ }^{33}$ The $\mathrm{Ru}-\mathrm{P}^{1}$ and $\mathrm{Ru}-\mathrm{P}^{2}$ bonds are much longer than the $\mathrm{Ru}-\mathrm{P}^{3}$ and $\mathrm{Ru}-\mathrm{P}^{4}$ bonds because of the strong trans influence of the hydride ligand (see Figure 1 for $\mathrm{P}^{1}-\mathrm{P}^{4}$ ).

In the $\mathrm{CO}_{2}$ insertion reaction without $\mathrm{PH}_{3}$ dissociation, $\mathrm{CO}_{2}$ approaches Ru to form a precursor complex, cis $-\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}{ }^{-}$ $\left(\mathrm{CO}_{2}\right) \mathbf{2 a}$. In 2a, the $\mathrm{Ru}-\mathrm{H}^{2}$ bond ( $1.633 \AA$ ) and the $\mathrm{Ru}-\mathrm{P}^{4}$ bond ( $2.410 \AA$ ) are only 0.018 and $0.006 \AA$ longer than those of $\mathbf{1 a}$, respectively, and the other moiety has almost the same geometry as that of $\mathbf{1 a}$. The $\mathrm{CO}_{2}$ moiety also little distorts. The $\mathrm{C}-\mathrm{H}^{2}$ distance $\left(2.919 \AA\right.$ ) and the $\mathrm{Ru}-\mathrm{O}^{1}$ distance $(4.522 \AA$ ) are quite long. Consistent with these features, the stabilization energy by $\mathrm{CO}_{2}$ coordination is only $2.6 \mathrm{kcal} / \mathrm{mol}$, as usually observed in the precursor complex of the $\mathrm{CO}_{2}$ insertion into metal-hydride and metal-alkyl bonds. ${ }^{8,34}$

In the transition state $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3}}$, only one imaginary frequency of $413 \mathrm{i} \mathrm{cm}{ }^{-1}$ was calculated. The eigenvector with this imaginary frequency mainly involves the approach of $\mathrm{O}^{1}$ to Ru and the elimination of $\mathrm{H}^{2}$ from Ru (See Supporting Information). These geometry changes are consistent with the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond. In $\mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}}$, the $\mathrm{Ru}-\mathrm{H}^{2}$ bond considerably lengthens by $0.503 \AA$ and the $\mathrm{C}-\mathrm{H}^{2}$ distance shortens to 1.190 $\AA$, which is very close to the $\mathrm{C}-\mathrm{H}$ bond of the formate anion. Also, the OCO angle significantly bends and both $\mathrm{C}-\mathrm{O}$ bonds considerably lengthen. These features indicate that the $\mathrm{Ru}-\mathrm{H}^{2}$

[^3]

Figure 2. Geometry changes in the reductive elimination of formic acid from $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{4} \mathbf{3 a}$. Bond distances are in angstroms and bond angles in degrees. In parentheses are the energy differences from 3a (kcal/mol; DFT(B3LYP)/BS-II/DFT(B3LYP)/BS-I calculation). The $\mathrm{PH}_{3}$ ligands at a perpendicular position of the $\mathrm{P}^{3}-\mathrm{Rh}-\mathrm{H}^{1}$ plane are omitted for brevity.
bond is much weakened and the formate anion has been almost formed at $\mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}}$. However, the $\mathrm{Ru}-\mathrm{O}^{1}$ distance ( $2.802 \AA$ ) is much longer than the usual Ru -formate bond, showing that the $\mathrm{Ru}-\mathrm{O}^{1}$ bond has not been sufficiently formed. This is because it is difficult for the $\mathrm{Ru}(\mathrm{II})$ complex to take a sevencoordinate structure and the $\mathrm{Ru}-\mathrm{O}^{1}$ bond cannot be formed without complete breaking of the $\mathrm{Ru}-\mathrm{H}$ bond. As a result, a significantly high activation barrier ( $E_{\mathrm{a}}=29.3 \mathrm{kcal} / \mathrm{mol}$ ) was calculated, where the $E_{\mathrm{a}}$ value is defined as an energy difference between $\mathbf{T S}_{2 \mathbf{2}-\mathbf{3 a}}$ and 2a.

The insertion product $\mathbf{3 a}$ is a monodentate formate complex which takes a six-coordinate pseudo-octahedral structure. Its $\mathrm{Ru}-\mathrm{O}^{1}$ distance ( $2.127 \AA$ ) is shorter than the experimental value reported for $\mathrm{RuH}\left(\eta^{2}-\mathrm{O}_{2} \mathrm{CH}\right)\left(\mathrm{PPh}_{3}\right)_{3},{ }^{17}$ probably because the $\mathrm{Ru}-$ $\mathrm{O}^{1}$ bond of the monodentate formate complex is stronger than that of the bidentate formate complex, $\mathrm{RuH}\left(\eta^{2}-\mathrm{O}_{2} \mathrm{CH}\right)\left(\mathrm{PPh}_{3}\right)_{3}$.
$\mathrm{PH}_{3}$ dissociation from cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ occurs with a destabilization energy of $24.8 \mathrm{kcal} / \mathrm{mol}$ to yield cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3} \mathbf{1 b}$. Though this destabilization energy is somewhat large, a bulky phosphine would dissociate from $\mathrm{Ru}(\mathrm{II})$ with a smaller destabilization energy. ${ }^{18} \mathrm{CO}_{2}$ coordinates with $\mathbf{1 b}$, affording cis$\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{CO}_{2}\right) \mathbf{2 b}$ with a stabilization energy of $4.6 \mathrm{kcal} /$ mol. In 2b, the $\mathrm{Ru}-\mathrm{O}^{1}$ and $\mathrm{C}-\mathrm{H}^{2}$ distances are rather long, being 2.615 and $2.903 \AA$, respectively. These geometrical features are similar to those of $\mathbf{2 a}$. In $\mathbf{2 b}, \mathrm{CO}_{2}$ is inserted into the $\mathrm{Ru}-\mathrm{H}$ bond through the transition state $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}$, to yield a monodentate formate complex, $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3} \mathbf{3 b}$. The eigenvector with an imaginary frequency $\left(226 \mathrm{icm}^{-1}\right)$ exhibits geometry changes consistent with the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond. The geometrical features of $\mathbf{T S}_{\mathbf{2 b} \mathbf{3 b}}$ resemble well those of $\mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}}$, except that the $\mathrm{Ru}-\mathrm{P}^{3}$ and $\mathrm{Ru}-\mathrm{O}^{1}$ bonds are significantly shorter than those of $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$. These shorter bonds would arise from the lesser steric repulsion between $\mathrm{CO}_{2}$ and $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}$ in $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}$ than that in $\mathbf{T S}_{\mathbf{2} \mathbf{a}-\mathbf{3} \mathbf{a}}$. The activation energy was calculated to be $10.3 \mathrm{kcal} / \mathrm{mol}$, which is much smaller than that for $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$. The insertion product $\mathbf{3 b}$ takes a five-coordinate square-pyramidal structure, since $\mathrm{Ru}(\mathrm{II})$ takes
a $\mathrm{d}^{6}$ electron configuration. The $\mathrm{Ru}-\left(\eta^{1}-\mathrm{OCOH}\right)$ moiety resembles well that of $\mathbf{3 a}$.

From these results, it is clearly concluded that $\mathrm{CO}_{2}$ is inserted into the $\mathrm{Ru}-\mathrm{H}$ bond with a large $E_{\mathrm{a}}$ value in cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ but with a small $E_{\mathrm{a}}$ value in cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}$.
4.2. Reductive Elimination of Formic Acid from $\operatorname{RuH}\left(\eta^{1}-\right.$ $\mathbf{O C O H})\left(\mathbf{P H}_{3}\right)_{n}(\boldsymbol{n}=3$ or 4$)$. $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{4} 3 \mathrm{a}$ and $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3} \mathbf{3 b}$ undergo the reductive elimination of formic acid $(\mathrm{HCOOH})$, as shown in Figures 2 and 3, respectively. Starting from 3a, the reductive elimination takes place through a three-membered transition state $\mathbf{T S}_{3 \mathrm{a}-\mathbf{6 a}}$ to afford Ru$\left(\mathrm{PH}_{3}\right)_{4}+\mathrm{HCOOH} \mathbf{6 a}$. In $\mathbf{T S}_{3 \mathrm{a}-6 \mathbf{a}}$, only one imaginary frequency of $1118 \mathrm{icm}^{-1}$ is calculated, and its eigenvector mainly involves the approach of $\mathrm{H}^{1}$ to $\mathrm{O}^{1}$. In this $\mathbf{T S}_{\mathbf{3 a}-\mathbf{6 a}}$, the $\mathrm{Ru}-\mathrm{O}^{1}$ bond considerably lengthens by $0.351 \AA$ and the $\eta^{1}$-formate ligand significantly moves downward so that the $\mathrm{O}^{1}$ atom approaches the $\mathrm{H}^{1}$ atom. However, the $\mathrm{Ru}-\mathrm{H}^{1}$ bond little lengthens and the $\mathrm{O}-\mathrm{H}^{1}$ distance is still very long ( $1.673 \AA$ ). These features indicate that the $\mathrm{Ru}-\mathrm{O}^{1}$ bond much weakens but the $\mathrm{Ru}-\mathrm{H}^{1}$ bond has not been broken yet, and the new $\mathrm{O}-\mathrm{H}$ bond formation has not been completed yet. In other words, the $\mathrm{O}^{1}-\mathrm{H}^{1}$ bond formation does not occur enough to compensate the energy destabilization by the $\mathrm{Ru}-\mathrm{O}^{1}$ bond weakening. As a result, the $E_{\mathrm{a}}$ value is very large ( $44.8 \mathrm{kcal} / \mathrm{mol}$ ). In this reductive elimination, the product is considered to be $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{4}+$ HCOOH 6a, since the $\operatorname{Ru}(0)$ complex tends to take a fourcoordinate structure. Further discussion of this reductive elimination is stopped here, because the reductive elimination more easily takes place via a different reaction course, as will be discussed below.

The $\eta^{1}$-formate complex $\mathbf{3 a}$ isomerizes to $\mathbf{4 a}$ by the rotation of $\eta^{1}$-formate about the $\mathrm{C}-\mathrm{O}^{1}$ bond, as shown in Scheme 1. In 4a, the $\mathrm{O}^{2}$ atom takes a position near the $\mathrm{H}^{1}$ atom (see Scheme 1 for $\mathrm{O}^{1}, \mathrm{O}^{2}$, and $\mathrm{H}^{1}$ ). This isomerization occurs via the transition state $\mathbf{T S}_{\mathbf{3 a}-\mathbf{4 a}}$. In $\mathbf{T S}_{\mathbf{3 a}-\mathbf{4 a}}$, only one imaginary frequency (164i $\mathrm{cm}^{-1}$ ) is calculated, and its eigenvector mainly involves the rotation of the $\mathrm{O}^{2} \mathrm{CH}^{2}$ moiety about the $\mathrm{C}-\mathrm{O}^{1}$ bond. In this


Figure 3. Geometry changes in the reductive elimination of formic acid from $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3} \mathbf{3 b}$. Bond distances are in angstroms and bond angles in degrees. In parentheses are the energy differences from 3b (kcal/mol; DFT(B3LYP)/BS-II//DFT(B3LYP)/BS-I calculation). The $\mathrm{PH}_{3}$ ligands at a perpendicular position of the $\mathrm{P}^{3}-\mathrm{Rh}-\mathrm{H}^{1}$ plane are omitted for brevity.

Scheme 1

transition state, the dihedral angle between the $\mathrm{C}-\mathrm{O}^{2}-\mathrm{H}^{2}$ and the $\mathrm{Ru}-\mathrm{O}^{1}-\mathrm{C}$ planes is about $90^{\circ}$, while the geometry of the other part little changes. Consistent with the smalll geometry changes, the isomerization easily occurs with a much smaller $E_{\mathrm{a}}$ value of $6.6 \mathrm{kcal} / \mathrm{mol}$.

From 4a, two types of reductive elimination are considered to occur; one takes place through a three-membered transition state $\mathbf{T S}_{4 \mathrm{a}-6 \mathrm{a}}$ which needs a considerably large $E_{\mathrm{a}}$ value of 43.2 $\mathrm{kcal} / \mathrm{mol}$ (the imaginary frequency of $1038 \mathrm{i} \mathrm{cm}^{-1}$ ). In this $\mathbf{T S}_{4 \mathrm{a}-6 \mathrm{a}}, \mathrm{Ru}-\mathrm{O}^{1}, \mathrm{O}^{1}-\mathrm{H}^{1}$, and $\mathrm{Ru}-\mathrm{H}$ distances are slightly longer than those of $\mathbf{T S}_{\mathbf{3 a}-\mathbf{6 a}}$, while the geometry of the other moiety is almost the same as that of $\mathbf{T S}_{3 \mathbf{a}-\mathbf{4} \mathbf{a}}$. The other type of reductive elimination proceeds through a five-membered transition state $\mathbf{T S}_{\mathbf{4 a}-5 \mathbf{a}}$ which needs a moderate $E_{\mathrm{a}}$ value of $25.5 \mathrm{kcal} /$ mol (the imaginary frequency of $558 \mathrm{i} \mathrm{cm}^{-1}$ ). $\mathbf{T S}_{4 \mathrm{a}-5 \mathrm{a}}$ is considerably different from $\mathbf{T S}_{\mathbf{4 a}-\mathbf{6 a}}$, as follows: (1) the Ru $\mathrm{O}^{1}$ distance moderately lengthens by $0.12 \AA$, indicating that the $\mathrm{Ru}-\mathrm{O}^{1}$ bond has not been broken yet; (2) the $\mathrm{O}^{1}$ atom moderately moves downward; (3) the $\mathrm{H}^{1}$ atom moderately moves toward the $\mathrm{O}^{2}$ atom; and (4) the $\mathrm{O}^{2}-\mathrm{H}^{1}$ distance (1.152 $\AA$ ) is close to the normal $\mathrm{O}-\mathrm{H}$ bond of HCOOH . These features indicate that the $\mathrm{H}-\mathrm{O}$ bond is easily formed in this $\mathbf{T S}_{\mathbf{4 a}-\mathbf{5 a}}$ with moderate geometry changes, unlike $\mathbf{T S}_{4 \mathbf{a}-\mathbf{6 a}}$. As a result, the five-membered reductive elimination easily occurs through $\mathbf{T S}_{\mathbf{4 a}-5 \mathrm{a}}$ with a smaller $E_{\mathrm{a}}$ value than that of three-membered reductive elimination.

The product, $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{4}(\mathrm{HCOOH}) \mathbf{5 a}$, of this reductive elimination is a $\mathrm{Ru}(0)$ complex of HCOOH , which resembles well the transition state $\mathbf{T S}_{\mathbf{4 a}-\mathbf{5 a}}$. Actually, $\mathbf{5 a}$ is slightly more stable than $\mathbf{T S}_{\mathbf{4 a}-\mathbf{5 a}}$ by only $0.6 \mathrm{kcal} / \mathrm{mol}$. The HCOOH dissociation from 5a causes destabilization in energy by ca. $7 \mathrm{kcal} / \mathrm{mol}$. This
means that a Lewis base such as triethylamine is necessary to release formic acid from Ru , as experimentally known. ${ }^{10}$

Starting from $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3} \mathbf{3 b}$, the reductive elimination of HCOOH also takes place through a three-membered transition state $\mathbf{T S}_{\mathbf{3 b}-\mathbf{6} \mathbf{b}}$, as shown in Figure 3. In $\mathbf{T S}_{\mathbf{3 b}-\mathbf{6} \mathbf{b}}$, the $\mathrm{O}^{1}$ atom slightly moves downward from the $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{3}$ plane and the $\mathrm{H}^{1}$ atom considerably moves toward the $\mathrm{O}^{1}$ atom. The geometry of the $\mathrm{Ru}-\mathrm{O}^{1}-\mathrm{H}^{1}$ moiety resembles well those of $\mathbf{T S}_{\mathbf{3 a - 6 a}}$ and $\mathbf{T S}_{\mathbf{4 a}-6 \mathbf{a}}$. Accordingly, the $E_{\mathrm{a}}$ value is very large ( $39.8 \mathrm{kcal} / \mathrm{mol}$ ).

Also in $\mathbf{3 b}$, the $\eta^{1}$-formate ligand can rotate about the $\mathrm{Ru}-$ $\mathrm{O}^{1}$ bond, to yield the isomer $\mathbf{4 b}$ through the transition state $\mathbf{T S}_{\mathbf{3 b}-\mathbf{4 b}}$ like the isomerization of $\mathbf{3 a}$ to $\mathbf{4 a}$. The formate complex 4b undergoes the $\mathrm{H}-\mathrm{OCOH}$ reductive elimination via either three-membered $\mathbf{T S}_{\mathbf{4 b}-\mathbf{6} \mathbf{b}}$ or five-membered $\mathbf{T S}_{\mathbf{4 b}-\mathbf{5 b}} . \mathbf{T S}_{\mathbf{4 b}-\mathbf{6 b}}$ resembles well $\mathbf{T S}_{\mathbf{3 b}-\mathbf{6 b}}$, and the $E_{\mathrm{a}}$ value is very large (40.4 $\mathrm{kcal} / \mathrm{mol})$. However, $\mathbf{T S}_{\mathbf{4 b}-5 \mathrm{~b}}$ resembles $\mathbf{T S}_{\mathbf{4 a}-5 \mathrm{a}}$ and the $E_{\mathrm{a}}$ value is moderate $(17.5 \mathrm{kcal} / \mathrm{mol})$.

In the three-membered reductive elimination, the product, Ru$\left(\mathrm{PH}_{3}\right)_{3}+\mathrm{HCOOH} \mathbf{6 b}$, is less stable than $\mathbf{T S}_{\mathbf{4 b}-\mathbf{6}}$. This means that some product complex should exist between $\mathbf{T S}_{\mathbf{4 b}-\mathbf{6} \mathbf{b}}$ and 6a. However, we omitted further examination, because this type of reductive elimination is not favorable and the five-membered reductive elimination occurs more easily. In the five-membered reductive elimination, the geometry of the product $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{3^{-}}$ ( HCOOH ) $\mathbf{5 b}$ is similar to that of $\mathbf{T S}_{\mathbf{4} \mathbf{b}-\mathbf{5 b}}$, and therefore, an energy difference between $\mathbf{T S}_{\mathbf{4 b}-\mathbf{5 b}}$ and $\mathbf{5 b}$ is very small (only $0.4 \mathrm{kcal} / \mathrm{mol}$ ). The HCOOH dissociation from $\mathbf{5 b}$ gives rise to a destabilization energy of $27.1 \mathrm{kcal} / \mathrm{mol}$, to yield $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{3}+$ HCOOH 6b, like 5a. These results again indicate that Lewis base is necessary for this HCOOH dissociation.
4.3. Oxidative Addition of $\mathbf{H}_{\mathbf{2}}$ to $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{n}(n=3$ or 4). $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{4} \mathbf{6 a}$ and $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{3} \mathbf{6 b}$ do not have a hydride ligand. Thus, the oxidative addition of $\mathrm{H}_{2}$ to $\mathbf{6 a}$ and $\mathbf{6 b}$ (eq 5) must occur to form the active species cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{n}$ 1. We investigated the $\mathrm{H}_{2}$ oxidative addition but failed to optimize the geometry of the transition state. This reaction is significantly exothermic; the exothermicity ( $E_{\text {exo }}$ ) is 31.9 and $38.1 \mathrm{kcal} / \mathrm{mol}$ for $\mathbf{1 a}$ and $\mathbf{1 b}$, respectively. From these results, it is reasonably concluded that the oxidative addition of $\mathrm{H}_{2}$ easily occurs with




8a (27.4)



Six-membered $\sigma$-bond metathesis


Figure 4. Geometry changes in the $\sigma$-bond metathesis of $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}$ with $\mathrm{H}_{2}$, in which $\mathrm{H}_{2}$ is at a position trans to $\mathrm{H}^{1}$. Bond distances are in angstroms and bond angles in degrees. In parentheses are the energy differences from $\mathbf{3 a}(\mathrm{kcal} / \mathrm{mol}$; DFT(B3LYP)/BS-II//DFT(B3LYP)/BS-I calculation). See Figure 3 for $\mathbf{T S}_{\mathbf{3 b}-\mathbf{4 b}}$ and $\mathbf{4 b}$. The $\mathrm{PH}_{3}$ ligands at a perpendicular position of the $\mathrm{P}^{3}-\mathrm{Rh}^{-} \mathrm{H}^{1}$ plane are omitted for brevity.
no barrier. A similar result was theoretically reported in the oxidative addition of $\mathrm{H}_{2}$ to $\mathrm{Ru}\left(\mathrm{PH}_{3}\right) 4 .{ }^{33}$ Moreover, the oxidative addition does not need to occur in the catalytic cycle, since the $\sigma$-bond metathesis of $\operatorname{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{n}$ with $\mathrm{H}_{2}$ more easily occurs than the reductive elimination and the active species is reproduced through the $\sigma$-bond metathesis, as will be discussed below. Thus, we stopped further investigation of this oxidative addition.
4.4. $\sigma$-Bond Metathesis of $\operatorname{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{n}(n=3$ or 4) with $\mathbf{H}_{2}$. In the $\sigma$-bond metathesis of $\operatorname{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)$ $\left(\mathrm{PH}_{3}\right)_{4}$ 3a with $\mathrm{H}_{2}, \mathrm{PH}_{3}$ must be substituted for $\mathrm{H}_{2}$, to yield $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right)$. We failed to optimize the transition state of associative substitution of $\mathrm{H}_{2}$ for $\mathrm{PH}_{3}$, since one $\mathrm{PH}_{3}$ dissociated from Ru during the geometry optimization of the transition state. This result suggests that the associative substitution of $\mathrm{H}_{2}$ for $\mathrm{PH}_{3}$ would not occur, probably because 3a is coordinatively saturated and the seven-coordinate structure is very unstable in the $\mathrm{Ru}(\mathrm{II})$ complex. Thus, the dissociative substitution of $\mathrm{H}_{2}$ for $\mathrm{PH}_{3}$ was investigated here. The $\mathrm{PH}_{3}$ dissociation gives rise to a destabilization energy of $19.1 \mathrm{kcal} /$ mol to afford a coordinatively unsaturated complex $\operatorname{RuH}\left(\eta^{1}-\right.$ $\mathrm{OCOH})\left(\mathrm{PH}_{3}\right)_{3} \mathbf{3 b}$ (see Figure 4). This destabilization energy is smaller than the activation barrier of any reductive elimination of $\mathrm{H}-\mathrm{OCOH}$ from 3 a , showing that the $\mathrm{PH}_{3}$ dissociation occurs more easily than the $\mathrm{H}-\mathrm{OCOH}$ reductive elimination.
$\mathrm{H}_{2}$ coordinates with $\mathbf{3 b}$, to afford a molecular hydrogen complex, $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right) 7$ a, with a stabilization energy of $7.6 \mathrm{kcal} / \mathrm{mol}$. In 7a, the $\mathrm{H}^{\alpha}-\mathrm{H}^{\beta}$ bond distance ( 0.782 $\AA$ ) is slightly longer than the normal $\mathrm{H}-\mathrm{H}$ bond (see Figure 4 for $\mathrm{H}^{\alpha}$ and $\mathrm{H}^{\beta}$ ), and the geometry of the $\mathrm{Ru}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}$ moiety is almost the same as that of $\mathbf{3 a}$, as shown in Figure 4. These features indicate that the $\mathrm{H}^{\alpha}-\mathrm{H}^{\beta}$ bond is little activated by Ru and the coordinate bond of $\mathrm{H}_{2}$ is weak. Starting from 7a, the four-membered $\sigma$-bond metathesis takes place through $\mathbf{T S}_{7 \mathrm{a}-8 \mathrm{a}}$ which exhibits only one imaginary frequency of 1252 i $\mathrm{cm}^{-1}$. The eigenvector with the imaginary frequency mainly
involves the approach of $\mathrm{H}^{\beta}$ to $\mathrm{O}^{1}$ but little involves the approach of $\mathrm{H}^{\alpha}$ to Ru . The $\mathrm{H}^{\alpha}-\mathrm{H}^{\beta}$ bond lengthens by $0.276 \AA$, while the $\mathrm{Ru}-\mathrm{H}^{\alpha}$ and $\mathrm{O}^{1}-\mathrm{H}^{\beta}$ distances are much longer than the normal $\mathrm{Ru}-\mathrm{H}$ and $\mathrm{O}-\mathrm{H}$ bond distances, respectively, showing that the new $\mathrm{Ru}-\mathrm{H}^{\alpha}$ and $\mathrm{O}^{1}-\mathrm{H}^{\beta}$ bonds have not been completely formed at $\mathbf{T S}_{7 \mathrm{a}-8 \mathrm{a}}$. As a result, the $E_{\mathrm{a}}$ value is considerably large ( $24.8 \mathrm{kcal} / \mathrm{mol}$ ). This four-membered $\sigma$-bond metathesis is similar to the previously reported four-membered $\sigma$-bond metathesis of $\mathrm{Rh}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{2}$ with $\mathrm{H}_{2}{ }^{12 \mathrm{a}}$ and the $\mathrm{H}-\mathrm{H}$ splitting by $\mathrm{PdH}(\mathrm{OH})\left(\mathrm{NH}_{3}\right) .{ }^{15 \mathrm{a}}$

Isomerization of 7a to 7b easily proceeds via a transition state $\mathbf{T S}_{7 \mathrm{a}-7 \mathrm{~b}}$ with a small activation barrier of only $3.4 \mathrm{kcal} / \mathrm{mol}$ (an imaginary frequency of $167 \mathrm{i} \mathrm{cm}^{-1}$ ). The $\sigma$-bond metathesis from $\mathbf{7 b}$ also occurs through a four-membered transition state $\mathbf{T S}_{\mathbf{7 b}-\mathbf{8 b}}$ with a very large $E_{\mathrm{a}}$ value of $29.3 \mathrm{kcal} / \mathrm{mol}$ (an imaginary frequency of $1184 \mathrm{i} \mathrm{cm}^{-1}$ ).
The five-coordinate formate complex $\mathbf{4 b}$, which is discussed in Figure 3, also undergoes coordination of $\mathrm{H}_{2}$ to yield 7b, as shown in Figure 4. From 7b, the four-membered $\sigma$-bond metathesis might occur through $\mathbf{T S}_{7 \mathbf{b}-\mathbf{8 b}}$. However, this reaction needs a considerably large $E_{\mathrm{a}}$ value (see above and Figure 4). Thus, the $\sigma$-bond metathesis starting from $\mathbf{4 b}$ is ruled out here.

Also, 7a isomerizes to $\mathbf{7 c}$ through a transition state $\mathbf{T S}_{7 \mathbf{a}-\mathbf{7}} \mathbf{c}$, which needs an $E_{\mathrm{a}}$ of $8.5 \mathrm{kcal} / \mathrm{mol}$. From 7c, $\sigma$-bond metathesis proceeds through a six-membered transition state $\mathbf{T S}_{\mathbf{7 c}-8 \mathrm{c}}$ (Figure 4). The eigenvector with the imaginary frequency ( $764 \mathrm{i} \mathrm{cm}^{-1}$ ) mainly involves the approach of $\mathrm{H}^{\beta}$ to $\mathrm{O}^{2}$ and that of $\mathrm{H}^{\alpha}$ to Ru . In $\mathbf{T S}_{7 \mathrm{c}-\mathbf{8 c}}$, the $\mathrm{H}^{\alpha}-\mathrm{H}^{\beta}$ and $\mathrm{Ru}-\mathrm{O}^{1}$ distances lengthen by 0.290 and $0.066 \AA$, respectively, the $\mathrm{Ru}-\mathrm{H}^{\alpha}$ distance shortens by $0.117 \AA$, the $\mathrm{Ru}-\mathrm{H}^{1}$ bond lengthens by $0.046 \AA$, and the $\mathrm{O}^{2}-$ $\mathrm{H}^{\beta}$ distance shortens to $1.183 \AA$. These geometrical changes indicate that the $\mathrm{H}^{\alpha}-\mathrm{H}^{\beta}$ bond is considerably weakened and the new $\mathrm{Ru}-\mathrm{H}^{\alpha}$ and $\mathrm{O}^{2}-\mathrm{H}^{\beta}$ bonds have been almost formed. The activation energy was calculated to be $8.2 \mathrm{kcal} / \mathrm{mol}$, which is much less than those of the four-membered metathesis and the three-membered and five-membered reductive eliminations.



7d (1.7)



Six-membered $\sigma$-bond metathesis


Figure 5. Geometry changes in the $\sigma$-bond metathesis of $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}$ with $\mathrm{H}_{2}$, in which $\mathrm{H}_{2}$ is at a position cis to $\mathrm{H}^{1}$. Bond distances are in angstroms and bond angles in degrees. In parentheses are the energy differences from 7a (kcal/mol; DFT(B3LYP)/BS-II//DFT(B3LYP)/BS-I calculation). The $\mathrm{PH}_{3}$ ligands at a perpendicular position of the $\mathrm{P}^{3}-\mathrm{Rh}-\mathrm{H}^{1}$ plane are omitted for brevity.

From these results, it should be concluded that the six-membered $\sigma$-bond metathesis is the easiest reaction path to afford formic acid. Darensbourg and Ovalles previously suggested that the formation of formic acid might occur through either the formateassisted heterolytic cleavage of $\mathrm{H}_{2}$ or the reductive elimination of formic acids concomitant with the oxidative addition of $\mathrm{H}_{2}$ to W. ${ }^{7}$ The former reaction is essentially the same as the sixmembered $\sigma$-bond metathesis presented here. Also, Morris et al. ${ }^{13}$ and Crabtree et al. ${ }^{14}$ experimentally proposed that the ligand-assisted $\mathrm{H}-\mathrm{H}$ splitting occurred through a six-membered interaction, which is essentially the same as the present sixmembered $\sigma$-bond metathesis. Milet et al. ${ }^{15 \mathrm{~b}}$ also theoretically investigated the ligand-assisted $\mathrm{H}-\mathrm{H}$ splitting through a multimembered interaction which is similar to our six-membered $\sigma$-bond metathesis. The geometry of the product complex RuH$\left(\mathrm{PH}_{3}\right)_{3}(\mathrm{HCOOH}) \mathbf{8 c}$ is similar to that of $\mathbf{T S}_{7 \mathrm{c}-8 \mathrm{c}}$. Consistent with this result, $\mathbf{8 c}$ is only $0.4 \mathrm{kcal} / \mathrm{mol}$ more stable than $\mathbf{T S}_{7 \mathbf{c}-\mathbf{8 c}}$ and less stable than 7 c by $7.8 \mathrm{kcal} / \mathrm{mol} .{ }^{35}$ Thus, the sixmembered $\sigma$-bond metathesis via $\mathbf{T S}_{7 \mathbf{c}-\mathbf{8}}$ is endothermic and the reverse reaction easily occurs, which again indicates that Lewis base is necessary in the reaction.

In this $\sigma$-bond metathesis, the $\mathrm{Ru}-\mathrm{H}^{\alpha}$ bond is formed at a position trans to $\mathrm{H}^{1}$ (hydride). This geometry is unfavorable because of the strong trans influence of the H ligand. Actually, the $\mathrm{Ru}-\mathrm{H}^{\alpha}$ bonds in $\mathbf{T S}_{7 \mathrm{c}-\mathbf{8 c}}$ and $\mathbf{8 c}$ are much longer than the $\mathrm{Ru}-\mathrm{H}$ bond of 3a. This unfavorable situation disappeared if

[^4]the $\sigma$-bond metathesis occurred in 7d (Figure 5) in which the $\eta^{1}$-formate ligand is at a position trans to $\mathrm{H}^{1}$. Thus, we investigated the isomerization of 7 a to $7 \mathbf{d}$ followed by the $\sigma$-bond metathesis of $\mathbf{7 d}$, as shown in Figure 5. This isomerization occurs via $\mathbf{T S}_{7 \mathrm{a}-7 \mathrm{~d}}$ with an $E_{\mathrm{a}}$ value of $17.7 \mathrm{kcal} / \mathrm{mol}$. This isomerization corresponds to the associative substitution of $\mathrm{H}^{\alpha}-\mathrm{H}^{\beta}$ for $\mathrm{H}^{\gamma}-\mathrm{H}^{\delta}$. In $\mathbf{T S}_{7 \mathrm{a}-7 \mathrm{~d}}$, the $\mathrm{H}^{\gamma}-\mathrm{H}^{\delta}$ moiety is much distant from Ru and it does not seem to interact with Ru. Only the approach of $\mathrm{H}^{\alpha}-\mathrm{H}^{\beta}$ to Ru is observed but the movement of $\mathrm{H}^{\gamma}-\mathrm{H}^{\delta}$ is not observed in the eigenvector with imaginary frequency ( $259 \mathrm{i} \mathrm{cm}^{-1}$ ). In $7 \mathbf{d}$, the $\mathrm{H}^{\alpha}-\mathrm{H}^{\beta}$ bond distance ( 0.868 $\AA$ ) is much longer, the $\mathrm{Ru}-\mathrm{H}_{2}$ distance is much shorter, and the $\mathrm{Ru}-\mathrm{O}^{1}$ and $\mathrm{Ru}-\mathrm{H}^{1}$ bonds are longer than those of $7 \mathbf{a}$. These features show that $\mathrm{H}_{2}$ more strongly and $\eta^{1}$-formate less strongly coordinates with Ru , which is interpreted in terms of a strong trans influence of $\mathrm{H}^{1}$ in 7a and 7d. From 7d, the four-membered $\sigma$-bond metathesis occurs through $\mathbf{T S}_{7 \mathrm{~d}-8 \mathrm{~d}}$ with an $E_{\mathrm{a}}$ value of $16.3 \mathrm{kcal} / \mathrm{mol}$. Also, 7 d undergoes the isomerization followed by either four-membered $\left(\mathbf{T S}_{7 \mathrm{e}-8 \mathrm{e}}\right)$ or six-membered $\left(\mathbf{T S}_{7 \mathrm{e}-\mathbf{8 f}}\right)$ $\sigma$-bond metathesis with an $E_{\mathrm{a}}$ value of 21.9 or $0.5 \mathrm{kcal} / \mathrm{mol}$, respectively (see Figure 5). The $E_{\mathrm{a}}$ value for the $\mathbf{7 d} \rightarrow \mathbf{7 e}$ isomerization is also very small $(2.4 \mathrm{kcal} / \mathrm{mol})$. Though both six-membered and four-membered $\sigma$-bond metatheses require a lower $E_{\mathrm{a}}$ value than those of $\mathbf{7 a}$ as expected, the $7 \mathbf{a} \rightarrow \mathbf{7 d}$ isomerization requires a larger $E_{\mathrm{a}}$ value $(17.7 \mathrm{kcal} / \mathrm{mol})$ than the $\mathbf{7 a} \rightarrow \mathbf{7 c}$ isomerization ( $8.5 \mathrm{kcal} / \mathrm{mol}$ ) followed by the sixmembered $\sigma$-bond metathesis of $7 \mathbf{c}(8.2 \mathrm{kcal} / \mathrm{mol})$. From these results, it is clearly concluded that we can neglect the reaction course involving the $\mathbf{7 a} \rightarrow \mathbf{7 d}$ isomerization followed by $\sigma$-bond


Figure 6. Energy changes in the $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$-catalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid. In parentheses are the energy differences from the sum of reactants ( $\mathrm{kcal} / \mathrm{mol}$; DFT(B3LYP)/BS-II//DFT(B3LYP)/BS-I calculation).
metathesis, and that formic acid is produced through the $\mathbf{7 a} \rightarrow$ 7c isomerization followed by the six-membered $\sigma$-bond metathesis via $\mathbf{T S}_{7 \mathrm{c}-8 \mathrm{c}}$.
4.5. Energy Changes in the Ru-Catalyzed Hydrogenation of $\mathbf{C O}_{2}$ into Formic Acid. We have completed all the preparations to discuss energy changes along the $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ catalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid. ${ }^{36}$ Above results indicate that (1) the six-membered $\sigma$-bond metathesis is the easiest reaction course to yield formic acid from the ruthenium(II) formate complex, while the substitution of $\mathrm{H}_{2}$ for $\mathrm{PH}_{3}$ must occur to perform the $\sigma$-bond metathesis; and (2) if the substitution of $\mathrm{H}_{2}$ for $\mathrm{PH}_{3}$ cannot occur, not the $\sigma$-bond metathesis but the five-membered $\mathrm{H}-\mathrm{OCOH}$ reductive elimination must take place as the last step. On the basis of these results, the following conclusions are presented about the reaction course: If $\mathrm{PH}_{3}$ does not dissociate from Ru , the reaction proceeds through the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of cis$\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ followed by the five-membered $\mathrm{H}-\mathrm{OCOH}$ reductive elimination from $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{4}$; i.e., $\mathbf{1 a} \rightarrow \mathbf{2 a} \rightarrow$ $\mathrm{TS}_{2 \mathrm{a}-3 \mathrm{a}} \rightarrow \mathbf{3 a} \rightarrow \mathrm{TS}_{3 \mathrm{a}-4 \mathrm{a}} \rightarrow 4 \mathrm{a} \rightarrow \mathrm{TS}_{4 \mathrm{a}-5 \mathrm{a}} \rightarrow \mathbf{5 a} \rightarrow \mathbf{6 a} \rightarrow \mathbf{1 a}$ +HCOOH , in which the rate-determining step is the $\mathrm{CO}_{2}$ insertion ( $E_{\mathrm{a}}=29.3 \mathrm{kcal} / \mathrm{mol}$ ), as shown in Figure 6. However, if $\mathrm{PH}_{3}$ can dissociate from 3a, the reaction mechanism changes. In this case, not the $\mathrm{H}-\mathrm{OCOH}$ reductive elimination but the six-membered $\sigma$-bond metathesis takes place, since $\mathrm{H}_{2}$ coordi-

[^5]nates with Ru after $\mathrm{PH}_{3}$ dissociation to afford $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)$ $\left(\mathrm{PH}_{3}\right)\left(\mathrm{H}_{2}\right)$ and the six-membered $\sigma$-bond metathesis of this complex takes place with a smaller $E_{\mathrm{a}}$ value than the fivemembered $\mathrm{H}-\mathrm{OCOH}$ reductive elimination. As a result, the reaction proceeds through $\mathbf{1 a} \rightarrow \mathbf{2 a} \rightarrow \mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}} \rightarrow \mathbf{3 a} \rightarrow \mathbf{3 b} \rightarrow$ $\mathbf{7 a} \rightarrow \mathbf{T S}_{7 \mathrm{a}-7 \mathrm{c}} \rightarrow \mathbf{7 c} \rightarrow \mathbf{T S}_{7 \mathrm{c}-8 \mathrm{c}} \rightarrow \mathbf{8 c} \rightarrow \mathbf{1 b}+\mathrm{HCOOH}$, in which the rate-determining step is also the $\mathrm{CO}_{2}$ insertion $\left(E_{\mathrm{a}}=\right.$ $29.4 \mathrm{kcal} / \mathrm{mol}$ ) and the second largest barrier is the $\mathrm{PH}_{3}$ dissociation in $\mathbf{3 a}(19.1 \mathrm{kcal} / \mathrm{mol})$. If $\mathrm{PH}_{3}$ dissociates from 1a, the catalytic reaction takes place through the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}$ followed by the sixmembered $\sigma$-bond metathesis; $\mathbf{1 b} \rightarrow \mathbf{2 b} \rightarrow \mathbf{T S}_{\mathbf{2 b} \mathbf{- 3 b}} \rightarrow \mathbf{3 b} \rightarrow$ $7 \mathrm{a} \rightarrow \mathrm{TS}_{7 \mathrm{a}-7 \mathrm{c}} \rightarrow \mathbf{7 c} \rightarrow \mathbf{T S}_{7 \mathrm{c}-8 \mathrm{c}} \rightarrow \mathbf{8 c}$, in which the ratedetermining step is the $\mathrm{CO}_{2}$ insertion ( $E_{\mathrm{a}}=10.3 \mathrm{kcal} / \mathrm{mol}$ ). From these results, it should be clearly concluded that if phosphine dissociates from Ru , this catalytic reaction easily proceeds. Actually, Jessop et al. experimentally reported that the addition of excess phosphine suppressed the reaction. ${ }^{10}$ Thus, the use of solvent that facilitates phosphine dissociation is recommended. Also, the ruthenium(II) complex that has three phosphine ligands is expected to be a good catalyst.
4.6. Electronic Process of the $\mathbf{C O}_{2}$ Insertion into the Ru(II) $-\mathbf{H}$ Bond. As described above, the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond is the rate-determining step. Also, the sixmembered $\sigma$-bond metathesis is of considerable importance, since the reaction course would be changed if this $\sigma$-bond metathesis was neglected. Thus, it is worthwhile to investigate electronic processes of these reactions. As shown in Figure 7, C atomic population considerably increases and $\mathrm{O}^{1}$ and $\mathrm{O}^{2}$ atomic populations moderately increase in both insertion reactions of $\mathbf{2 a}$ and $\mathbf{2 b}$, while Ru atomic population significantly decreases in both, where natural bond orbital population was adopted. ${ }^{37}$ However, $\mathrm{H}^{2}$ atomic population little changes. These features suggest that the charge transfer to $\mathrm{CO}_{2}$ from $\mathrm{H}^{2}$ occurs considerably, and at the same time, $\mathrm{H}^{2}$ is provided electrons from Ru , as shown in Scheme 2. The other important feature observed in Figure 7 is that the populations little change upon
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(A) $\mathrm{CO}_{2}$ insertion in the six-coordinate cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$

(B) $\mathrm{CO}_{2}$ insertion in the five-coordinate cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}$

Figure 7. Population changes in the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{n}\left(n=3\right.$ and 4): Natural bond orbital population ${ }^{37}$ with DFT(B3LYP)/BS-II//DFT(B3LYP)/BS-I calculation. A positive value represents an increase in the population relative to the precursor complex.

## Scheme 2


going to the product from the TS. This result clearly indicates that formate is almost formed at the TS, as displayed by geometry changes.

It is noted that $\mathrm{O}^{1}$ atomic population increases at the TS but then decreases at the product in the insertion reaction of $\mathbf{2 a}$, while it little decreases at the product in the insertion reaction of $\mathbf{2 b}$. This difference suggests that the charge transfer from $\mathrm{O}^{1}$ to Ru is difficult at $\mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}}$ in the insertion reaction of $\mathbf{2 a}$, probably because the $\mathrm{O}^{1}$ atom cannot easily approach Ru due to the congested geometry of $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$ (see the geometry changes shown in Figure 1).

The orbital energy changes are compared between two insertion reactions, as shown in Figure 8. An important difference is that the HOMO becomes less stable upon going from $2 \mathbf{a}$ to $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$ but becomes more stable upon going from $\mathbf{2 b}$ to $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}$. The next notable difference is that $\phi_{50}$ and $\phi_{51}$ significantly rise in energy upon going from $\mathbf{2 a}$ to $\mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}}$, while $\phi_{41}$ and $\phi_{42}$ moderately rise in energy upon going from $\mathbf{2 b}$ to $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}$ (note that $\phi_{50}$ and $\phi_{51}$ of $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$ correspond to $\phi_{41}$ and $\phi_{42}$ of $\mathbf{T S}_{\mathbf{2 b} \mathbf{b} \mathbf{b}}$, respectively). These differences are
responsible for the larger $E_{\mathrm{a}}$ value of the insertion reaction of 2a. Their contour maps are shown in Figure 8. In $\mathbf{T S}_{\mathbf{2} \mathbf{a}-\mathbf{3}}$, the HOMO involves considerable antibonding overlaps between Ru d and O p orbitals and between Rud and H 1s orbitals. On the other hand, the HOMO of $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}$ involves the antibonding overlap between Ru d and O p orbitals and nonbonding interaction between Ru d and H 1 s orbitals. As a result, the HOMO of $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$ is much less stable than that of $\mathbf{T S}_{\mathbf{2 b} \mathbf{- 3 b}}$. The next question is why the antibonding interaction between Ru d and H 1s orbitals is involved in $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$ but not in $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}$. This would be interpreted in terms that the $\mathrm{H}^{2}$ ligand is forced to take the position that suffers from the antibonding interaction with the Ru d orbital because of the congested structure of $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$. In $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3} \mathbf{b}}, \mathrm{CO}_{2}$ can take a better position, due to the less congested structure, and therefore, the reaction system can avoid the unfavorable situation in which $\mathrm{H}^{2}$ gives rise to an antibonding overlap between Ru d and H 1 s orbitals. The difference in behavior of molecular orbitals at lower energy is also understood in terms of the $\mathrm{Ru}-\mathrm{O}^{1}$ bonding interaction, as follows: $\phi_{50}$ and $\phi_{51}$ of $\mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}}$ involve weaker $\mathrm{Ru}-\mathrm{O}^{1}$ bonding than $\phi_{41}$ and $\phi_{42}$ of $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}$, due to the longer $\mathrm{Ru}-\mathrm{O}^{1}$ distance in $\mathbf{T S}_{\mathbf{2 a}-\mathbf{3 a}}$ than that in $\mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}$. The long $\mathrm{Ru}-\mathrm{O}^{1}$ distance in $\mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}}$ also arises from the congested structure.
4.7. Electronic Process of the $\boldsymbol{\sigma}$-Bond Metathesis. In both six-membered and four-membered $\sigma$-bond metatheses, $\mathrm{H}^{\beta}$ atomic population significantly decreases, while $\mathrm{H}^{\alpha}$ atomic population moderately increases, as shown in Figure 9. These population changes clearly show that both $\sigma$-bond metatheses occur through heterolytic bond cleavage of $\mathrm{H}-\mathrm{H}$. This feature is essentially the same as that of the ligand-assisted $\mathrm{H}_{2}$ splitting in $\operatorname{Ir}(\mathrm{III})$ and $\mathrm{Pd}($ II $)$ complexes previously reported. ${ }^{13-15}$

Significant differences are observed between four-membered and six-membered $\sigma$-bond metatheses: the Ru atomic population gradually increases in the six-membered $\sigma$-bond metathesis, while it little increases at the TS but suddenly increases at the product in the four-membered $\sigma$-bond metathesis. Also, the $\mathrm{O}^{1}$ atomic population increases at the TS and then decreases at the product in the four-membered $\sigma$-bond metathesis, while it little changes in the six-membered $\sigma$-bond metathesis. These features suggest that electron distribution smoothly changes in the sixmembered $\sigma$-bond metathesis but it does not in the fourmembered metathesis. This difference is interpreted in terms of orbital interaction, as follows: In the four-membered $\sigma$-bond metathesis, the $\mathrm{O}^{1}$ lone pair orbital of formate must change its direction toward $\mathrm{H}^{\beta}$ to form the $\mathrm{O}-\mathrm{H}$ bond, as shown in Scheme 3. This direction change weakens the CT interaction with Ru and decreases the Ru atomic population. Approach of formate to $\mathrm{H}_{2}$ induces the polarization of the $\mathrm{H}_{2}$ moiety so that the $\mathrm{H}^{\alpha}$ atom becomes more negatively charged and the $\mathrm{H}^{\beta}$ atom becomes more positively charged. This polarization enhances the charge transfer from $\mathrm{H}^{\alpha}$ to Ru . Thus, the Ru atomic population little changes at the TS, due to the compensation of these two CT interactions. At the product, the $\mathrm{H}^{\alpha}$ ligand completely becomes hydride. Since the hydride ligand substantially donates electrons to Ru , the Ru atomic population considerably increases at the product. In the six-membered $\sigma$-bond metathesis, the situation is different; since the $\mathrm{O}^{2}$ atom has a lone pair orbital which expands toward the $\mathrm{H}^{\beta}$ atom in $7 \mathbf{c}$, the $\mathrm{O}^{2}-\mathrm{H}^{\beta}$ bond can be smoothly formed without considerable weakening of the $\mathrm{Ru}-\mathrm{O}^{1}$ bond in the six-membered $\sigma$-bond metathesis. Because of these smooth bond formations, the electron distribution smoothly changes in this $\sigma$-bond metathesis. The above discussion suggests that the $\mathrm{O}-\mathrm{H}$ bond is more easily formed in the six-membered $\sigma$-bond metathesis than in the four-


Figure 8. Energy levels and contour maps of several important molecular orbitals in the $\mathrm{CO}_{2}$ insertion in $\operatorname{cis}-\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{n}(n=3$ and 4): DFT-(B3LYP)/BS-II/DFT(B3LYP)/BS-I calculation. Contour values are from $-0.525 \mathrm{e} \cdot \mathrm{au}^{-3}$ to $0.525 \mathrm{e} \cdot \mathrm{au}^{-3}$ at intervals of $0.025 \mathrm{e} \cdot \mathrm{au}^{-3}$. Solid lines represent positive and zero contours, and dotted lines represent negative contours.
membered $\sigma$-bond metathesis. Actually, the formate moiety is more stable in $\mathbf{T S}_{\mathbf{7 c}-\mathbf{8 c}}$ than in $\mathbf{T S}_{7 \mathbf{a}-\mathbf{8 a}}$ by ca $10 \mathrm{kcal} / \mathrm{mol}$, where the calculation was carried out for the formate anion whose geometry was taken to be the same as that in $\mathbf{T S}_{7 \mathbf{a}-\mathbf{8 a}}$ or $\mathbf{T S}_{7 \mathbf{c}-\mathbf{8} \mathbf{c}}$. This energy difference roughly corresponds to the difference in $E_{\mathrm{a}}$ between six-membered and four-membered $\sigma$-bond metatheses. From these results, it is concluded that the sixmembered $\sigma$-bond metathesis more easily takes place than the four-membered one because the $\mathrm{O}-\mathrm{H}$ bond is more easily formed in the former than in the latter.

## 5. Conclusions

All of the possible elementary steps involved in rutheniumcatalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid were theoretically investigated with the DFT(B3LYP) method. Since cis$\mathrm{RuH}_{2}(\mathrm{PMe})_{4}$ was experimentally used as a catalyst, we adopted cis $-\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ as a catalyst model. Important results are summarized, as follows: (1) the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond occurs with difficulty in cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ but occurs easily in cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{3}$; (2) the $\mathrm{H}-\mathrm{OCOH}$ reductive elimination requires a very large $E_{\mathrm{a}}$ value ( 40.3 and $44.8 \mathrm{kcal} / \mathrm{mol}$ for $n=$ 3 and 4, respectively) for the three-membered transition state but a moderately large $E_{\mathrm{a}}$ value ( 25.5 and $17.5 \mathrm{kcal} / \mathrm{mol}$ for $n$ $=3$ and 4 , respectively) for the five-membered transition state; (3) though the four-membered $\sigma$-bond metathesis of cis-RuH-$\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\left(\mathrm{H}_{2}\right)$ requires a very large $E_{\mathrm{a}}$ value ( $24.8 \mathrm{kcal} /$ mol ), the six-membered $\sigma$-bond metathesis occurs with a
moderate $E_{\mathrm{a}}$ value ( $8.2 \mathrm{kcal} / \mathrm{mol}$ ); and (4) the phosphine dissociation in cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ and cis- $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{4}$ is necessary for the $\sigma$-bond metathesis.

From the above results, we can conclude that the reaction mechanism depends on the reaction conditions; when $\mathrm{PH}_{3}$ cannot dissociate from Ru, the precursor complex for the $\sigma$-bond metathesis cannot be formed and only the $\mathrm{H}-\mathrm{OCOH}$ reductive elimination can take place. Thus, the hydrogenation of $\mathrm{CO}_{2}$ into formic acid takes place through the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}$ followed by the $\mathrm{H}-\mathrm{OCOH}$ reductive elimination, where the rate-determining step is the $\mathrm{CO}_{2}$ insertion ( $E_{\mathrm{a}}=29.3 \mathrm{kcal} / \mathrm{mol}$ ). When $\mathrm{PH}_{3}$ can dissociate from Ru in cis$\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{4}, \mathrm{CO}_{2}$ is much more easily inserted into the $\mathrm{Ru}-\mathrm{H}$ bond with a much smaller $E_{\mathrm{a}}$ value $(10.3 \mathrm{kcal} / \mathrm{mol})$, and the resultant complex, cis- $\mathrm{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}$, easily undergoes the six-membered $\sigma$-bond metathesis with $\mathrm{H}_{2}$, where the ratedetermining step is the $\mathrm{CO}_{2}$ insertion. Apparently, the $\mathrm{PH}_{3}$ dissociation facilitates this catalytic reaction. Actually, it was experimentally reported that addition of excess $\mathrm{PMe}_{3}$ suppressed the reaction. ${ }^{10 \mathrm{c}}$

From the above results, the use of solvent that facilitates phosphine dissociation is recommended in this catalytic reaction. Also, the $\mathrm{Ru}(\mathrm{II})$ complex that has three phosphine ligands is expected to be a good catalyst.

It should be noted that the six-membered $\sigma$-bond metathesis is the easiest reaction course to produce formic acid. If this $\sigma$-bond metathesis was neglected, the five-membered reductive

(A) Four-membered $\sigma$-bond metathesis

(B) Six-membered $\sigma$-bond metathesis

Figure 9. Population changes in the $\sigma$-bond metathesis of $\mathrm{RuH}\left(\eta^{1}-\right.$ $\mathrm{OCOH})\left(\mathrm{PH}_{3}\right)_{3}$ with $\mathrm{H}_{2}$ : Natural bond orbital population ${ }^{37}$ with DFT-(B3LYP)/BS-II//DFT(B3LYP)/BS-I calculation. A positive value represents an increase in the population relative to the $\mathrm{H}_{2}$ complex.
elimination of $\mathrm{H}-\mathrm{OCOH}$ became the easiest reaction to yield formic acid, since the five-membered reductive elimination needs a smaller $E_{\mathrm{a}}$ value ( $17.5 \mathrm{kcal} / \mathrm{mol}$ ) than does the fourmembered $\sigma$-bond metathesis ( $E_{\mathrm{a}}=24.8 \mathrm{kcal} / \mathrm{mol}$ ). Thus, the neglect of the six-membered $\sigma$-bond metathesis leads to a different conclusion of the reaction mechanism, as follows: the $\mathrm{CO}_{2}$ hydrogenation occurs through the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond followed by the five-membered $\mathrm{H}-\mathrm{OCOH}$ reductive elimination. This clearly shows the importance of the sixmembered $\sigma$-bond metathesis. The six-membered $\sigma$-bond metathesis is essentially the same as the formate-assisted $\mathrm{H}_{2}$ activation which was previously proposed by Darensbourg et al. ${ }^{7}$ As discussed above, we should take the six-membered

Scheme 3


Four-membered $\sigma$-bond metathesis


Six-membered $\sigma$-bond metathesis
$\sigma$-bond metathesis into consideration when discussing the reaction mechanism of transition metal catalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid; for instance, the six-membered $\sigma$-bond metatheses of $\operatorname{Rh}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{2}$ and $\left[\mathrm{RhH}\left(\eta^{1}-\mathrm{OCOH}\right)\right.$ $\left.\left(\mathrm{PH}_{3}\right)_{3}\right]^{+}$occur with nearly no barrier. ${ }^{38}$ The detailed investigation is in progress now.

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Supporting Information Available: Figures of the DFT-(B3LYP)-optimized geometries and energy changes in the oxidative addition of $\mathrm{H}_{2}$ to $\mathrm{Ru}\left(\mathrm{PH}_{3}\right)_{n}(n=3$ and 4), figures of the eigenvectors with imaginary frequency (DFT(B3LYP)/BSI) in the transition states of the $\mathrm{CO}_{2}$ insertion into the $\mathrm{Ru}-\mathrm{H}$ bond of cis- $\mathrm{RuH}_{2}\left(\mathrm{PH}_{3}\right)_{n}(n=3$ and 4), the reductive elimination of formic acid from $\operatorname{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{n}(n=3$ and 4$)$, the $\sigma$-bond metathesis of $\operatorname{RuH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}$ with $\mathrm{H}_{2}$, and the isomerizations of $\mathbf{3 a} \rightarrow \mathbf{4 a}, \mathbf{3 b} \rightarrow \mathbf{4 b}, \mathbf{7 a} \rightarrow \mathbf{7 b}, \mathbf{7 a} \rightarrow \mathbf{7 c}, 7 \mathrm{a} \rightarrow$ $\mathbf{7 d}$, and $\mathbf{7 d} \rightarrow \mathbf{7 e}$. Energy levels of several important molecular orbitals for $\mathbf{2 a}, \mathbf{2 b}, 7 \mathbf{a}, \mathbf{7 c}, \mathbf{T S}_{2 \mathrm{a}-3 \mathrm{a}}, \mathbf{T S}_{\mathbf{2 b}-\mathbf{3} \mathbf{b}}, \mathbf{T S}_{7 \mathbf{a}-8 \mathrm{a}}$, and $\mathbf{T S}_{7 \mathrm{c}-8 \mathrm{c}}$ and their contour maps (PDF). This material is available free of charge via the Internet at http://pubs.acs.org.

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    $\ddagger$ Department of Applied Chemistry and Biochemistry, Faculty of Engineering.
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[^4]:    (35) A similar feature was found in the reaction between dihydrido-(quinoline-8-acyliminol)bis(triphenylphosphine)iridium(III) and $\mathrm{H}_{2}$, in which the ligand-assisted $\mathrm{H}-\mathrm{H}$ splitting and the ligand-assisted $\mathrm{H}-\mathrm{H}$ coupling reversibly occur.

[^5]:    (36) We estimated the activation energies of several important steps with the MP4(SDQ) method to examine if the DFT(B3LYP) method yields reliably the activation barrier. When the DFT(B3LYP) and MP4(SDQ) methods yielded considerably different values, we further calculated it with the $\operatorname{CCSD}(\mathrm{T})$ method. In the $\mathrm{CO}_{2}$ insertion step $\left(\mathbf{2 b} \rightarrow \mathbf{T S}_{\mathbf{2 b}-\mathbf{3 b}}\right)$, the $E_{\mathrm{a}}$ value was calculated to be $10.3,14.2$, and $11.0 \mathrm{kcal} / \mathrm{mol}$ with DFT(B3LYP), MP4(SDQ), and CCSD(T) methods, respectively, showing that the DFT(B3LYP) value is similar to the $\operatorname{CCSD}(\mathrm{T})$ value. In the five-membered reductive elimination ( $\mathbf{4 b} \rightarrow \mathbf{T S}_{\mathbf{4 b}-\mathbf{5 b}}$ ), the $E_{\mathrm{a}}$ value was calculated to be $17.5 \mathrm{kcal} / \mathrm{mol}$ with the DFT(B3LYP) method and $16.0 \mathrm{kcal} / \mathrm{mol}$ with the MP4(SDQ) method. In the isomerization of 7a to 7c, the $E_{\mathrm{a}}$ value was calculated to be $8.5 \mathrm{kcal} / \mathrm{mol}$ with the DFT(B3LYP) method and $9.5 \mathrm{kcal} /$ mol with the MP4(SDQ) method. In the six-membered $\sigma$-bond metathesis ( $7 \mathbf{c} \rightarrow \mathbf{T S}_{\mathbf{7 c}-8 \mathbf{c}}$ ), the $E_{\mathrm{a}}$ value was calculated to be $8.2 \mathrm{kcal} / \mathrm{mol}$ with the DFT(B3LYP) method and $9.3 \mathrm{kcal} / \mathrm{mol}$ with the MP4(SDQ) and CCSD(T) methods. These results suggest that the DFT(B3LYP) method, as well as MP4(SDQ) and CCSD(T) methods, provides a reliable activation barrier.

[^6]:    (38) This six-membered $\sigma$-bond metathesis was not investigated in the theoretical work of $\mathrm{Rh}(\mathrm{I})$-catalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid. ${ }^{12}$ We investigated the six-membered $\sigma$-bond metatheses of $\operatorname{Rh}\left(\eta^{1}-\mathrm{OCOH}\right)$ $\left(\mathrm{PH}_{3}\right)_{2}$ and $\left[\mathrm{RhH}\left(\eta^{1}-\mathrm{OCOH}\right)\left(\mathrm{PH}_{3}\right)_{3}\right]^{+}$with $\mathrm{H}_{2}$ and found that these reactions much more easily occurred with nearly no barrier than the four-membered $\sigma$-bond metathesis. These results suggest that $\mathrm{Rh}(\mathrm{I})$-catalyzed hydrogenation of $\mathrm{CO}_{2}$ into formic acid occurs with nearly no barrier and the six-membered bond metathesis of the formate complex should be taken into consideration when discussing the reaction mechanism of rhodium(I)- and rhodium(III)catalyzed hydrogenations of $\mathrm{CO}_{2}$ into formic acid.

